Angular dependent time delay in two-color XUV/IR photoemission of He and Ne

I A Ivanov^{1,2} and A S Kheifets¹

¹ Research School of Physics and Engineering, The Australian National University, Canberra ACT 0200, Australia and

² Center for Relativistic Laser Science, Institute for Basic Science (IBS), Gwangju 500-712, Republic of Korea

(Dated: June 6, 2017)

We solve the time dependent Schrödinger equation for a noble gas atom (He and Ne) driven by an ionizing XUV and dressing IR fields. From this solution we deduce an angular dependence of the photoemission time delay as measured by the RABBITT (Reconstruction of Attosecond Beating By Interference of Two-photon Transitions) technique. We use a recent angular resolved RABBITT measurement on helium [Phys. Rev. A **94**, 063409 (2016)] to test and calibrate our theoretical model. Based on this calibration, we find no significant difference between the time delay in He measured in the angular integrated RABBITT experiments [J. Phys. B **47**, 245003 and 245602 (2014)] and measured or calculated in the polarization axis direction. The angular dependence of the photoemission time delay of Ne is shown to be qualitatively different from He because of the different orbital character of the valence 2p orbital. The angular momentum projection dependence of the time delay in Ne is also investigated.

PACS numbers: 32.80.Rm, 32.80.Fb, 42.50.Hz

I. INTRODUCTION

A measurable time delay in laser driven atomic ionization has been discovered recently [1, 2]. Since the first pioneering experiments, the time-delay spectroscopy of laser-induced atomic ionization (attosecond chronoscopy) has become a rapidly developing field [3]. In a recent report, Heuser et al. [4] investigated an angular dependence of the photoemission time delay in helium as measured by the RABBITT (Reconstruction of Attosecond Beating By Interference of Two-photon Transitions) technique. The RABBITT technique builds on the interference of two ionization processes leading to the same photoelectron state by (i) absorption of ω_{2q-1} and ω or (ii) absorption of ω_{2q+1} and stimulated emission of ω . Both ionization processes lead to the appearance of a side band (SB), in between the one-photon harmonic peaks in the photoelectron spectrum. The sideband magnitude oscillates with the relative phase between the XUV and IR pulses [5, 6]

$$S_{2q}(\tau) = A + B\cos[2\omega\tau - C] \quad , \ C = \Delta\phi_{2q} + \Delta\theta_{2q} \quad , \ (1)$$

where $\tau = \varphi/\omega$ denotes the phase delay of the IR field. The term $\Delta \phi_{2q} = \phi_{2q+1} - \phi_{2q-1}$ denotes the phase difference between two neighbouring odd harmonics $2q \pm 1$ that is related to the finite-difference group delay of the attosecond pulse as $\tau_{2q}^{(\text{GD})} = \Delta \phi_{2q}/2\omega$. The additional term $\Delta \theta_{2q} = \theta_{2q+1}^{(-)} - \theta_{2q-1}^{(+)}$ arises from the phase difference of the atomic ionization amplitude for emission (-) and absorption (+) paths, respectively. This phase difference can be converted to the atomic delay

$$\tau_a = \Delta \theta_{2q} / 2\omega = \tau_W + \tau_{cc} , \qquad (2)$$

which contains the two distinct components [7]. Here τ_W is the Wigner-like time delay associated with the XUV absorption and τ_{cc} is a correction due to the continuum– continuum (CC) transitions in the IR field. The latter term, τ_{cc} , can also be understood as a coupling of the long-range Coulomb ionic potential and the laser field in the context of streaking [8, 9].

In the case of helium with only one $1s \to Ep$ photoemission channel, the Wigner time delay τ_W does not depend on the photoelectron detection angle relative to the polarization vector. The early investigations of the τ_{cc} correction [7] showed no dependence of τ_{cc} over various angular momentum paths in hydrogen, e.g. the transitions $s \to p \to s$ and $s \to p \to d$ showed τ_{cc} in excellent agreement. This would imply that the RABBITT measured time delay in He should be angular independent. This assumption was challenged in a recent experiment by Heuser et al. [4] in which the RABBITT technique was supplemented with the COLTRIMS (Cold Target Recoil Ion Momentum Spectroscopy) apparatus. This combination made it possible to relate the time delay to a specific photoelectron detection angle relative to the joint polarization axis of the XUV and IR pulses. The finding of Heuser et al. [4] is significant because the helium atom is often used as a convenient reference to determine the time delay in other target atoms. If the RABBITT measurement is not angular resolved, like in the experiments by Palatchi et al [10] or Guénot et al [11], the angular dependence of the time delay in the reference atom may compromise the accuracy of the time delay determination in other target atoms. However, in the present work, we demonstrate that the magnitude of the RABBITT signal is dropping off very rapidly, as $\cos^4 \theta$ away from the polarization direction and hence the angular integrated RABBITT measurement on He would return the time delay very close to that calculated or measured in the polarization direction.

In the case of Ne and heavier noble gases, both components of the measured time delay $\tau_a = \tau_W + \tau_{cc}$ are angular dependent. Indeed, for a one-photon transition from a bound *np*-orbital, there are two competing *s* and *d* continua which can lead to the angular dependent Wigner time delay τ_W [12–14]. Because of the propensity rule [15], the *d*-channel is strongly dominant except in the vicinity of its Cooper minimum. Such a minimum is absent in Ne. So the Wigner time delay should depend on the emission angle very weakly. Therefore any measurable angular variation of the time delay in Ne should be attributed almost entirely to the τ_{cc} component. The latter arises due to the competition of the CC transitions $d \rightarrow p$ or $d \rightarrow f$. This competition is analyzed in the present work.

II. THEORY AND NUMERICAL IMPLEMENTATION

We solve the TDSE for a helium atom described within the single active electron (SAE) approximation

$$i\partial\Psi(\boldsymbol{r})/\partial t = \left[\hat{H}_{\mathrm{atom}} + \hat{H}_{\mathrm{int}}(t)\right]\Psi(\boldsymbol{r}) ,$$
 (3)

where \hat{H}_{atom} is the Hamiltonian of the field-free atom with an effective one-electron potential [16]. The Hamiltonian $\hat{H}_{\text{int}}(t)$ describes the interaction with the external field and is written in the velocity gauge

$$\hat{H}_{\rm int}(t) = \boldsymbol{A}(t) \cdot \hat{\boldsymbol{p}} \quad , \quad \boldsymbol{A}(t) = -\int_0^t \boldsymbol{E}(t') \, dt'. \quad (4)$$

As compared to the alternative length gauge, this form of the interaction has a numerical advantage of a faster convergence.

The vector potential of the APT is modeled as the sum of 11 Gaussian pulses of altering polarity shifted by a half of the IR period $T = 2\pi/\omega$:

$$A_x(t) = \sum_{n=-5}^{5} (-1)^n A_n \exp\left(-2\ln 2\frac{(t-nT/2)^2}{\tau_x^2}\right) \\ \times \cos\left[\omega_x(t-nT/2)\right].$$
(5)

The amplitude of each pulse is defined as

$$A_n = A_0 \exp\left(-2\ln 2\frac{(nT/2)^2}{\tau_T^2}\right),$$

where A_0 is the vector potential amplitude related to the field intensity $I = (\omega^2/c^2)A_0^2$. The XUV central frequency is $\omega_x = 1.378$ au = 37.5 eV. The time constants $\tau_x = 0.14$ fs and $\tau_T = 4.83$ fs determine the length of an XUV pulse and the APT train, respectively. The field intensity of the APT is chosen at 5×10^8 W/cm² and the XUV frequency $\omega_x \simeq 25\omega$.

The vector potential of the IR pulse is modeled by the cosine squared envelope

$$A(t) = A_0 \cos^2\left(\frac{\pi(t-\tau)}{2\tau_{\rm IR}}\right) \cos[\omega(t-\tau)] , \qquad (6)$$

with an intensity of 3×10^{11} W/cm² and pulse duration of $\tau_{IR} = 14.5$ fs. The IR pulse is shifted relative to the APT by a variable delay $0 \le \tau \le 0.5T$. A positive delay, $\tau > 0$, corresponds to the IR pulse being delayed with respect to the center of the XUV pulse train. Further, the laser photon energy is $\omega = 0.05841$ au = 1.59 eV, which corresponds to a period of $T = 2\pi/\omega = 107$ au = 2.60 fs. The laser pulse duration is $\tau = 5.58T = 14.5$ fs.

To solve the TDSE, we follow the strategy tested in our previous works [17, 18]. The solution of the TDSE is presented as a partial wave series

$$\Psi(\boldsymbol{r},t) = \sum_{\substack{l=0\\|m| \le l}}^{L_{\max}} f_l(\boldsymbol{r},t) Y_{lm}(\theta,\phi)$$
(7)

with only $m = m_0$ momentum projections retained for the linearly polarized light. Here m_0 refers to the target orbital: $m_0 = 0$ for He 1s and $m_0 = 0, \pm 1$ for Ne 2p. The radial part of the TDSE is discretized on the grid with the stepsize $\delta r = 0.05$ a.u. in a box of the size $R_{\rm max} = 2000$ a.u. The number of partial waves in Eq. (7) was limited to $L_{\rm max} = 5$ which ensured convergence in the velocity gauge calculations.

Substitution of the expansion (7) into the TDSE gives a system of coupled equations for the radial functions $f_{l\mu}(r,t)$, describing evolution of the system in time. To solve this system, we use the matrix iteration method [20]. The ionization amplitudes $a(\mathbf{k})$ are obtained by projecting the solution of the TDSE at the end of the laser pulse on the set of the ingoing scattering states of the target Hamiltonian. Squared amplitudes $|a(\mathbf{k})|^2$ give the photoelectron spectrum in a given direction $\hat{\mathbf{k}}$ determined by the azimuthal angle θ_k .

After collecting the photoelectron spectra from TDSE in various directions, the SB intensity oscillation with the variable time delay between the APT and IR fields is fitted with the cosine function (1) using the non-linear Marquardt-Levenberg algorithm. The quality of the fit is very good with the errors in all three parameters not exceeding 1%.

III. RESULTS

A. Helium

The angular dependence of the parameters A, B and C in Eq. (1) for the SB20 is shown in Fig. 1. It follows from the soft photon approximation (SPA) [21] that the angular dependence of the $A = |\mathcal{M}_{k}^{(-)}|^{2} + |\mathcal{M}_{k}^{*(+)}|^{2}$ and $B = 2 \operatorname{Re} \left[\mathcal{M}_{k}^{(-)} \mathcal{M}_{k}^{*(+)} \right]$ parameters are simple $\cos^{4} \theta$ functions for an initial s-state,

$$A, B \propto |J_1(\boldsymbol{\alpha}_0 \cdot \boldsymbol{k})|^2 |\langle f|z|i \rangle|^2 \propto \cos^4 \theta_k \tag{8}$$

Here $\mathcal{M}_{k}^{(\pm)}$ are complex amplitudes for angle-resolved photoelectron produced by adding or subtracting an IR photon, respectively. In Eq. (8) we made a linear approximation to the Bessel function as the parameter



FIG. 1: (Color online) Angular dependence of the fitting parameters A, B, and C for the SB20 in He. The TDSE calculation is shown with the filled (red) circles and open (blue) circles, respectively. The insets show the variation of the A and B parameters near 90°. The $\cos^4 \theta_k$ fit to the A and B parameters is displayed with the solid line.

 $\alpha_0 = F_0/\omega^2$ is small in a weak IR field. This simple dependence fits very well both the *A* and *B* parameters. The only deviation occurs at large angles where the *B* parameter becomes negative while $\cos^4 \theta$ always remains positive (see insets of Fig. 1. The SPA also predicts no angular variation of the time delay. So angular dependent time delay and alteration of sign of the *B* parameter are both signs of breakdown of the SPA.

The group delay $\tau_{\rm GD}$ of the APT is zero in our approach since we consider Fourier limited attosecond pulses by setting $\phi_{2q+1} = 0$, for all integers q in the frequency comb. Hence the parameter C can be converted directly into the atomic time delay as $\tau_a = C/2\omega$ according to Eq. (1). The atomic time delay obtained in this fashion is given in Table I for the direction along the polarization axis, which we refer to as the zero angle for photoemission. To connect with Eq. (2) we also show the breakdown of the atomic delay into the Wigner time delay τ_W , which was computed separately by a one-photon RPAE program [22], and the extracted continuum-continuum delay τ_{cc} which we compare with an earlier calculation [7]. The discrepancy between the two CC quantities is reasonably small, less than ten attoseconds, even though the present result is obtained for He whereas the calculation [7] was performed for H. This reflects a universal nature of the CC correction which is not sensitive to the target *ns* orbital. The variation of the atomic time delay relative to the zero angle polarization direction $\Delta \tau = \tau_a(\theta_k) - \tau(0^\circ)$ is displayed in Fig. 2 for SB 18 to 24. In the same figure, we plot the experimental data and the lowest order perturbation theory (LOPT) calculation from Heuser et al. [4].



FIG. 2: (Color online) Variation of the time delay relative to the zero angle $\Delta \tau_a = \tau_a(\theta_k) - \tau_a(0^\circ)$ for SB 18, 20, 22, 24 (from left to right). The TDSE results are shown with the (green) asterisks. The LOPT calculation and experimental data from Heuser et al. [4] are visualized with the (blue) open circles and error bars, respectively.

In the experimentally accessible angular range of 0 to 65° , the angular variation of the time delay is rather small. It progressively decreases from about 60 as in SB18 to less than 30 as in SB24. It is expected that for higher sidebands it will be even smaller as the CC

phases for the s and d waves become indistinguishable in the high photon energy limit. Given the rapid drop of the magnitude A and B parameters in Eq. (1) with the detection angle as $\cos^4 \theta_k$, the angular averaged time delay $\bar{\tau}_a$ will be very close to that recorded in the polarization



FIG. 3: (Color online) Angular dependence of the fitting parameters A, B, and C for the SB20 in Ne. The TDSE calculation is shown with the filled (red) circles and open (blue) circles, respectively. The $\cos^4 \theta_k$ fit to the A and B parameters is displayed with the (red) solid line and the fit with actual anisotropy parameter $\beta = 0.3$ is shown by the thick solid line. The TDSE result for He is also shown for parameter C.

TABLE I: Atomic time delay τ_a and its various components τ_W and τ_{cc} in the \hat{z} direction for various side bands.

SB	$B \qquad n\omega \qquad E \ \tau_a \ (as) \ \tau_W \ (as)$				τ_{cc} (as) a	
n	eV	eV	TDSE	RPAE	(i)	(ii)
18	27.9	3.3	-85	231	-316	-315
20	31.0	6.4	-61	60	-121	-129
22	34.1	9.5	-46	30	-76	-83
24	37.2	12.6	-37	16	-53	-57

(i) Atomic delay minus Wigner delay

(ii) Fit to exact hydrogen calculation [7]

direction of light at the zero degree angle $\tau_a(\theta = 0)$. This allows to use the helium atom as a convenient standard both in the angular specific streaking and angular averaged RABBITT time delay measurements.



FIG. 4: (Color online) Variation of the atomic time delay relative to the zero emission angle $\Delta \tau_a = \tau_a(\theta_k) - \tau_a(0^\circ)$ for SB 18, 20, 22, 24 (from left to right) in neon. The TDSE results are shown with the (red) filled circles. The analogous calculation for He is displayed with the (blue) asterisks. The angular variation of the Wigner time delay $\Delta \tau_W = \tau_W(\theta_k) - \tau_W(0^\circ)$ in one-photon ionization is shown with open circles.

B. Neon

The angular dependence of the parameters A, B and C in Ne for the SB20 is shown in Fig. 3. This variation is qualitatively similar to that in He as displayed in Fig. 1. However, unlike in He, where the $\cos^4 \theta_k$ dependence of the statement of the stateme

dence fits both the A and B parameters very well, in Ne this dependence deviates noticeably from the TDSE calculation. This is so because the squared dipole matrix element $|\langle f|z|i\rangle|^2 \propto 1 + \beta P_2(\cos\theta_k)$ deviates from $\cos^2\theta_k$ for $\beta \neq 2$ which is the case of the Ne 2p shell where for the SB20 $\beta \approx 0.3$ [19]. In this case a more accurate fit is

provided by the second Legendre polynomial expression as shown in Fig. 3.

Even though the A and B parameters decrease very rapidly with the detection angle, this decrease is not as rapid in Ne as prescribed by the soft photon approximation. The C parameters both in Ne and He experience the drop of one unit of π . However, in Ne, this drop is more gradual in comparison with He.

Angular variation of time delay in neon for SB18 to 24 is shown in Fig. 4. The analogous set of He data is also plotted for the sake of comparison. The angular dependence of the time delay in Ne is more pronounced at small angles where the He data are virtually flat. The flattening of the angular dependence in Ne is also happening towards the higher order sidebands, but not as quickly as in He.

As it was mentioned in the introduction, both the components of the atomic time delay in Ne can be angular dependent. However, because of the lack of the Cooper minimum, the angular dependence of the Wigner time delay τ_W should be weak. This dependence is shown in Fig. 4 in comparison with the angular variation of the total atomic time delay τ_a . The Wigner time delay, calculated in the relativistic random-phase approximation [14] varies noticeably only in the lowest side band and this variation is significantly smaller that that of the total time delay in all the sidebands. This indicates that the angular variation of the measured time delay in Ne should be attributed almost solely to the τ_{cc} component. The latter arises due to the competition of the CC transitions $d \to p$ or $d \to f$. Unlike in helium, where the two CC transitions compete strongly only beyond the magic angle, this competition seems to be noticeable in Ne even at small angles.

To quantify this competition, we consider the case of m = 0 projection in the target orbital and adapt the parametrization of the ionization amplitudes similar to that suggested in Heuser et al. [4]:

$$\mathcal{M}_{\boldsymbol{k}}^{(\pm)} \propto Y_{10}(\boldsymbol{n}) + c_{fp}^{(\pm)} e^{i\phi_{fp}^{(\pm)}} Y_{30}(\boldsymbol{n}) , \qquad (9)$$

where $c_{fp}^{(\pm)}$ and $\phi_{fp}^{(\pm)}$ are the magnitude ratio and phase difference between the f and p partial wave components of the absorption (+) and emission (-) amplitudes, respectively. Fitting the angular dependence of the time delay in the SB18 for m = 0 is shown in Fig. 5. The values of the fitting parameters are $c_{fp}^{\pm} = 0.39, 1.68$ and $\phi_{fp}^{\pm} = 1.65, 0.54$. In comparison in SB20 of He, $c_{ds}^{\pm} = 0.67, 1.17$ and $\phi_{ds}^{\pm} = 0.082, 0.076$. In the high energy limit of He, $c_{ds}^{+} = 1/c_{ds}^{-} = \sqrt{4/5} \approx 0.89$ whereas for Ne this limit is $\sqrt{4/7} \approx 0.75$. The case of Ne seems to be farther away from the asymptotic limit in which no angular dependence should be observed. Even more contrasting is the phase difference in Ne which is an order of magnitude larger than in He.

Quite remarkably, the m = 0 angular dependence of the atomic time delay is very different from that summed



FIG. 5: (Color online) Angular dependent time delay in neon for SB18. The full TDSE calculation summed over all the mprojections is shown by the (red) filled circles whereas the m =0 calculation is visualized by the open circles. Parametric fit to the latter calculation with Eq. (9) is shown by the (blue) solid line

over all the m =projection. It is dominated by the sharp drop near the kinematic node of the Y_{30} spherical harmonic. This drop is all but disappeared in the angular dependence summed over all the *m*-projections because $Y_{3\pm 1}$ fill the node. Despite this difference, the parametrization (9) can still be employed meaningfully to quantify the competition of the CC transitions $d \to f$ and $d \to p$ because their strengths depend only on the radial integrals.

IV. CONCLUSION

In the present work we studied angular variation of the atomic time delay in the RABBIT measurement on helium and neon. We employed a numerical solution of the time-dependent Schrödinger equation for a single atomic electron driven by a combination of the XUV/IR fields with parameters similar to that used in a recent RABBITT measurement by Heuser et al. [4]. Our results for He compare favorably with this measurement. Based on this agreement, we make further predictions for neon which is yet to be measured in an angular resolved RABBITT experiment.

In comparison to He, the angular variation of time delay in Ne is more pronounced at small ejection angles relative to the polarization axis where the He time delay is essentially flat. This can be explained by a larger phase difference between the $d \rightarrow f$ and $d \rightarrow p$ CC transitions in the absorption and emission channel. The analogous phase difference between the $p \rightarrow d$ and $p \rightarrow s$ CC transitions in He is an order of magnitude smaller.

We also analyze the magnitude of the RABBITT signal in both targets and find it dropping off very rapidly away from the polarization direction. In He, the RAB-BITT signal drops as $\cos^4 \theta_k$, much faster than the usual dipole factor $\cos^2 \theta_k$. The difference between these two factors becomes particularly noticeable at large ejection angles: at $\theta_k = 70^\circ$ the one-photon angular factor leaves ~ 10% magnitude relative to the maximum whereas the two-photon factor leaves only ~ 1%. It is for this reason that Heuser et al. [4] were not able to extend their measurements beyond the ejection angle of 65°. However, because of the same reason, the angular integrated RAB-BITT measurements on He and Ne in [10, 11] could be compared directly with the time delay calculated along the polarization axis. In contrast, the angular variation of the atomic time delay in Ar was found noticeable in [10] as the angular averaged calculations were found much closer to the experiment than that in the polarization.

The angular dependence of the RABBITT time delay in molecules becomes even more pronounced because of an additional anisotropy relative to the molecular axis. This can be seen from a recent theoretical study on the hydrogen molecular ion [23]. Angular integrated RAB-BITT experiments have been reported on other molecules

- [1] M. Schultze *et al*, Science **328**(5986), 1658 (2010).
- [2] K. Klunder *et al*, Phys. Rev. Lett. **106**(14), 143002 (2011).
- [3] R. Pazourek, S. Nagele, and J. Burgdörfer, Rev. Mod. Phys. 87, 765 (2015).
- [4] S. Heuser, A. Jiménez Galán, C. Cirelli, C. Marante, M. Sabbar, R. Boge, M. Lucchini, L. Gallmann, I. Ivanov, A. S. Kheifets, et al., Phys. Rev. A 94, 063409 (2016).
- [5] H. Muller, Appl. Phys. B **74**, s17 (2002).
- [6] E. S. Toma and H. G. Muller, J. Phys. B 35(16), 3435 (2002).
- [7] J. M. Dahlström et al, Chem. Phys. 414, 53 (2013).
- [8] C.-H. Zhang and U. Thumm, Phys. Rev. A 84, 033401 (2011).
- [9] R. Pazourek, S. Nagele, and J. Burgdorfer, Faraday Discuss. 163, 353 (2013).
- [10] C. Palatchi et al, J. Phys. B 47(24), 245003 (2014).
- [11] D. Guénot et al, J. Phys. B 47(24), 245602 (2014).
- [12] J. M. Dahlström and E. Lindroth, J. Phys. B 47(12), 124012 (2014).
- [13] J. Wätzel, A. S. Moskalenko, Y. Pavlyukh, and J. Berak-

6

[24] and the work is underway to make this measurement angular resolved. So extension of the theory to complex molecules is warranted.

Acknowledgements

The authors are grateful to Luca Argenti, Álvaro Himenez Galán, Fernando Martín, Sebastian Heuser, Claudio Cirelli, Ursula Keller, Marcus Dahlström and Eva Lindroth for many stimulating discussion. We acknowledge support by the Australian Research Council in the form of the Discovery grant DP120101805. IA acknowledges support from the Institute for Basic Science, Gwangju, Republic of Korea, under IBS-R012-D1. Resources of the National Computational Infrastructure facility were employed.

dar, J. Phys. B 48(2), 025602 (2015).

- [14] A. S. Kheifets et al, Phys. Rev. A 94, 013423 (2016).
- [15] U. Fano, Phys. Rev. A **32**, 617 (1985).
- [16] A. Sarsa, F. J. Gálvez, and E. Buendia, Atomic Data and Nuclear Data Tables 88(1), 163 (2004).
- [17] I. A. Ivanov, Phys. Rev. A 83(2), 023421 (2011).
- [18] I. A. Ivanov and A. S. Kheifets, Phys. Rev. A 87, 033407 (2013).
- [19] K. Codling, R. G. Houlgate, J. B. West, and P. R. Woodruff, J. Phys. B 9(5), L83 (1976).
- [20] M. Nurhuda and F. H. M. Faisal, Phys. Rev. A 60(4), 3125 (1999).
- [21] A. Maquet and R. Taïeb, J. Modern Optics 54(13-15), 1847 (2007).
- [22] A. S. Kheifets, Phys. Rev. A 87, 063404 (2013).
- [23] V. V. Serov and A. S. Kheifets, Phys. Rev. A 93, 063417 (2016).
- [24] M. Huppert, I. Jordan, D. Baykusheva, A. von Conta, and H. J. Wörner, Phys. Rev. Lett. **117**, 093001 (2016).